

Noise and Interference Limited Systems

Noise Limited - range is signal power limited, BER decreases exponentially with SNR Interference Limited - probablistic based (fading, signal distortion, multipath), increasing transmit power doesn't improve BER very much since BER decreases linearly with SNR

Basics of link budgets

- Link budgets show how different components and propagation processes influence the available SNR
- Link budgets can be used to compute required transmit power, possible range of a system or required receiver sensitivity
- Link budgets can be easily set up using logarithmic power units (dB) dB = 10 log₁₀ (Pout/Pin)

A logarithmic scheme is a data compression technique scaling what would otherwise be ratios (out/in) of very large or very small quantities. Unfortunately this ends up hiding from our normal perception what are actually very small or very big ratios.

SINGLE LINK The link budget – a central concept



dB in general

When we convert a measure X into decibel scale, we always divide by a reference value X_{ref}:



The corresponding dB value is calculated as:

$$X|_{dB} = 10 \log \left(\frac{X|_{non-dB}}{X_{ref}|_{non-dB}}\right)$$

Note that this ratio has no units, it is dimensionless. It is annotated with dB only to inform us of the mathematics or compression technique that was used on the relative ratio of two numbers of the same units, i.e., apples/apples. There are 3 types of dB:

dB - the ratio and in the next slide we'll see power as dBw - power relative to Watt (W) dBm - power relative to milliwatt (mW)

Power

We usually measure power in Watt (W) and milliWatt [mW] The corresponding dB notations are dB and dBm



Decibels (dB) - Details

 $G_{dB} = 10 \log_{10} (P_{out}/P_{in})$

Gain is the inverse of Loss G = 1/L

Gain in dB = - Loss in dB $G_{dB} = - L_{dB}$

- $L_{dB} = -10 \log (P_{out} / P_{in}) = 10 \log (P_{in} / P_{out})$
- Since $P = V^2/R$ where P = power (Watts) dissipated across R = resistance/impedence where V = voltage across R then $G_{dB} = 10 \log[(V_{out}^2/R) / (V_{in}^2/R)] = 20 \log[V_{out} / V_{in}]$ given that the input and output impedances are the same
- 3 dB → power has been doubled (-3 dB is $\frac{1}{2}$ reduction) -10 dB → power has been reduced by a factor of 10 (0.1)
- dBw (decibel-Watt) gain referenced to 1 W
 dBm (decibel-milliWatt) gain referenced to 1 mW (10⁻³ W)
- + 30 dBm = 0 dBW 0 dBm = 30 dBW

Sensitivity level of GSM RX: 6.3×10^{-14} W = -132 dB or -102 dBm Bluetooth TX: 10 mW = -20 dB or 10 dBmGSM mobile TX: 1 W = 0 dB or 30 dBm**ERP** – Effective GSM base station TX: 40 W = 16 dB or 46 dBm Radiated Power Vacuum cleaner: 1600 W = 32 dB or 62 dBm takes antenna gains into account Car engine: 100 kW = 50 dB or 80 dBmTV transmitter (Hörby, SVT2): 1000 kW ERP = 60 dB or 90 dBm ERP Nuclear powerplant (Barsebäck): 1200 MW = 91 dB or 121 dBm

Amplification and attenuation



** as long as apples out is the same as apples in

Example: Amplification and attenuation



The total amplification of the (simplified) receiver chain (between A and B) is

$$G_{A,B}|_{dB} = 30 - 4 + 10 + 10 = 46 \text{ dB}$$

If 5 mW shows up at A, how much power appears at B? (Hint: either convert 5 mW to dB or convert the G = 46 dB to its relative #. Does it make any difference if the input to A is in dB or dBm?

need to convert just addition for dB just addition for dB_m

Categories of Noise

- Thermal Noise
- Intermodulation noise
- Crosstalk
- Impulse Noise

Noise Terminology

- Intermodulation noise occurs if signals with different frequencies share the same medium in association with some nonlinear device
 - Interference caused by a signal produced at a frequency that can be multiples of the sum or difference of original frequencies; result of nonlinear devices (a mixer, a diode, a dissimlar junction - just about all electronic devices are nonlinear)
- Crosstalk unwanted coupling between signal paths (excessive signal strength, no isolation, undesired mutual coupling, etc.)
- Impulse noise irregular pulses or noise spikes
 - RF Energy of short duration with relatively high amplitudes
 - Caused by external electromagnetic disturbances (lightning), or faults and flaws in the communications system
 - Not a big problem for analog data but the primary error source for digital transmission, may be minimized by the demodulation technique, noise blanker electronic circuits, antenna diversity.

Thermal Noise

- Thermal noise due to agitation of electrons
- Present in all electronic devices and transmission media (white noise)
- Function of temperature
- Cannot be eliminated (except at temperatures of absolute 0°K)
- Particularly significant for satellite
 communication (since the satellite frequencies don't have many other noise sources, thermal noise is the only normal source of noise)

Amount of thermal noise to be found in a bandwidth of 1 Hz for any device or conductor is:

$$N_0 = \mathrm{k}T(\mathrm{W/Hz})$$

- N_0 = noise power density in watts per 1 Hz of bandwidth
- $k = Boltzmann's constant = 1.3803 \times 10^{-23} J/K$
- T = temperature, in Kelvins (absolute temperature)

Thermal Noise

- Noise is assumed to be independent of frequency
- Thermal noise present in a bandwidth of *B* Hertz (in watts):

$N = \mathbf{k}TB$

The larger the bandwidth the larger the noise energy since (white) noise is uniform across the entire spectrum.

or in decibel-watts

 $N_{dBw} = 10 \log k + 10 \log T + 10 \log B$ $= -228.6 \, dB_w + 10 \log T + 10 \log B$

 $N_{\textit{dBm}} = -198.6 \text{ dB}_m + 10 \log T + 10 \log B$ for decibel-milliwatts

Expression E_b/N_0

a commonly used ratio in digital communications (dimensionless usually in dB)

Ratio of signal energy per bit to noise power density per Hz energy per bit $E_b = (Signal Power S)(Time to send 1 bit T_b)$ where $R = 1/T_b$

$$\frac{E_b}{N_0} = \frac{S/R}{N_0} = \frac{S}{kTR}$$
 (Signal Power) (Time for 1 bit)
Noise Power

- The bit error rate for digital data is a function of E_b/N_0
 - Given a value for E_b/N_o to achieve a desired error rate, parameters of this formula can be selected
 - As bit rate *R* increases, transmitted signal power (S) must increase to maintain required $E_b/N_o = W_{dBw} 10\log R 10\log k 10\log T (^{o}K)$
- Ratio doesn't depend on bandwidth as does Shannon's channel capacity (It is a normalized SNR measure, a SNR per bit. Used to compare BER for different modulation schemes without taking bandwidth into account spectral efficiency.)



Rewriting Shannon's Channel Capacity C wrt SNR (noise)

 $C = B \log_2(1 + S/N)$ S/N = 2 C/B - 1 thus

 $E_b/N_o = (B/C) (2^{C/B} - 1)$ derivation in Stallings page 113

Which allows us to the find the required noise ratio E_b/N_o for a given spectral efficiency C/B Spectral Efficiency = 6 bps/Hz then Eb/No = 10.5 = 10.21 dB

Noise sources

The noise situation in a receiver depends on several noise sources



Man-made noise

Noise Floor increasing with time will have an impact on the future of reliable communications



Receiver Noise: Equivalent Noise Source

To simplify the situation, we replace all noise sources with a single equivalent noise source.



The power spectral density of a noise source is usually given in one of the following three ways:

1) Directly [W/Hz]:

2) Noise temperature [Kelvin]:

3) Noise factor [no units]:

The relation between the three is

 $N_s = kT_s = kF_sT_0$

where *k* is **Boltzmann's constant** (1.38x10⁻²³ W/Hz) and T_0 is the, so called, **room temperature** of 290 K (17° C).



Noise Figure F

• Noise Figure (F) you might see noise figure as NF in dB NF = $10 \log_{10}(F)$

F = Measured Noise Power Out of Device at Room Temp Power Out of Device if Device Were Noiseless

- F is always greater than 1.
- Effective Noise Temperature (T_e)

 $T_e = (F - 1)T_o$ where T_o is ambient room temperature, typically 290°K to 300°K which is 63 °F to 75°F or 17 °C to 27 °C

A noiseless device has a F = 1 or T_e = 0K

Cascaded System Noise Figure - F_{sys}

• For a cascaded system, the noise figure of the overall system is calculated from the (non-dB) noise figures and gains of the individual components

which shows that the noise figure of the first active device in a cascaded system (usually F_1) is the most important part of a cascaded system in terms of the F_{sys} noise figure (1st active device's noise figure is far more important than the gain) Paragraph just below Equation 3.6 starting with the words Note that is in error, see textbook errata for page 39 errors.

• When passive (non-active) components such as transmission lines, attenuators, connectors, etc. are used in cascaded system noise calculations $F_{db} = L_{db} = -G_{db}$ or for linear (non-dB) parameters F = L = 1/Gthe noise figure F is the same as the loss L

(note that a positive loss/attenuation L in dB represents a negative gain G in dB) Thus for passive components the Noise Figure = Loss (attenuation) and the corresponding (non-dB) G for the device is 1/L as used in the above F_{sys} equation (note G and L are not in decibels for F_{sys}) A tool is available at http://www.pasternack.com/t-calculator-noise-figure.aspx

Noise Temperature for a System

 The overall equivalent temperature for a cascaded system has the same relationship as the noise figure, the T_e of the system is impacted the most by the first component's T₁

where the gains are in linear or relative values - NOT dB

 $F = (T_o + T_e) / T_o \text{ or } NF = 10 \log_{10} (1 + T_e/290) \text{ where To is room temperature}$ normally 290 °K

Communications System Analysis Noise Figure and Noise Temperature

 T_e and F are useful since the gains of the receiver stages are not needed to quantify the overall noise amplification of the receiver. If an antenna at room temperature is connected to the input of a receiver having a noise figure F, then the noise power at the output of the receiver referred to the input is simply F times the input noise power or

Pout = $F k T_o B = (1 + Te/To) k T_o B$

Te - effective noise temperature in degrees Kelvin To - room temperature in degrees Kelvin Noise Figure F = 1 + Te / To

Link Budget for a Receiver System

- Consider a cell phone receiver with a noise figure F = 4 that is connected to an antenna at room temperature using a coaxial cable with a loss L = 3 dB.
 - Compute the noise figure of the mobile receiver system as referred to the input of the antenna



A mobile receiver system with cable losses.

- For non active devices F = L (either dB or linear) the cable (a non-active device) noise factor is F = 3 dB = 2 or with a G = -3 dB = 0.5
- Keeping all values in linear rather than in dB, the receiver system has a noise figure $F_{1} = 2 \text{ or } 3 \text{ dB}$ $F_{2} = 4 \text{ or } 6.02 \text{ dB}$ $F_{1} = 2 \text{ or } 3 \text{ dB}$ $F_{2} = 4 \text{ or } 6.02 \text{ dB}$ $F_{1} = 1/F_{1} = 0.5 \text{ or } -3.01 \text{ dB}$ $F_{1} = 2 \text{ or } 3 \text{ dB}$ $F_{2} = 4 \text{ or } 6.02 \text{ dB}$

Communications Analysis Problem

For a mobile receiver system, determine the average output thermal noise power as referred to the input of the antenna terminals. The receiver system has a noise figure (F = 8 dB) and a bandwidth of 30 kHz. Assume $T_0 = 290$ °K

Solution: The effective noise temperature of the system $T_e = (F - 1)T_o = (8 - 1)300 = 2100 \text{ }^{\circ}\text{K}$

The overall system noise temperature due to the antenna is given by:

 $T_{TOTAL} = T_{ant} + T_{sys} = (290 + 2100) = 2390 \text{ °K}$

Since $P_o = (1 + T_e / T_o) k T_o B$ then the average output thermal noise power referred to the antenna terminals is given by

 $P_n = (1 + 2390/300)(1.38 \times 10^{-23})(300 \text{ }^{\circ}\text{K})(30,000 \text{ Hz}) = 1.11 \times 10^{-15} \text{ W} = -149.53 \text{ dBw} = -119.53 \text{ dBm}$

For the mobile receiver system, determine the required average signal strength at the antenna terminals to provide a SNR of 30 dB at the receiver output.

Solution:

From above, the average noise power is -119.53 dBm therefore the signal power must be 30 dB greater than the noise $P_s = SNR + (-119.53) = 30 - 119.53 = -89.53 dBm$

Receiver noise: Noise sources (2)

Antenna example



Power spectral density of the antenna noise is

 $N_a = 1.38 \times 10^{-23} \times 1600 = 2.21 \times 10^{-20}$ W/Hz = -196.6 dB[W/Hz]

and its noise factor is 5.52 or its noise figure is 7.42 dB

 $F_a = 1600/290 = 5.52 = 7.42 \text{ dB}$ at room temperature 290 K

Receiver noise: System noise



Due to a definition of noise factor (in this case) as the ratio of noise powers on the output versus on the input, when a resistor in room temperature (T_0 =290 K) generates the input noise, the PSD of the equivalent noise source (placed **at the input**) becomes

$$N_{sys} = k(F-1)T_0 \text{ W/Hz}$$
Don't use dB value! Equivalent noise temperature

Receiver noise: Several noise sources (1)

A simple example



After extraction of the noise sources from each component, we need to move them to one point.

When doing this, we must compensate for amplification and attenuation!



Pierce's rule

A passive attenuator, in this case a feeder line, has a noise figure equal to its attenuation. Also $L_f = 1/G$ required for cascaded noise figure calculations.



The isotropic antenna



The dipole antenna

$\lambda/2$ -dipole



This antenna does not radiate equally in all directions. Therefore, more energy is available in other directions.

THIS IS THE PRINCIPLE BEHIND WHAT IS CALLED *ANTENNA GAIN*. Most gain is broadside to the antenna with a null off of the ends of the antenna.

A dipole can be of any length, but the antenna patterns shown are only for the $\lambda/2$ -dipole.

Elevation pattern

Azimuth pattern

 Antenna pattern of isotropic antenna.

Antenna gain (principle)

Antenna gain is a relative measure.

We will use the isotropic antenna as the reference with units dB_i



Sometimes the notation dB_i is used for antenna gain (instead of dB).

The "i" indicates that it is the gain is relative to an isotropic antenna (which we will use in this course).

Another measure of antenna gain frequently encountered is **dBd**, which is relative to the $\lambda/2$ dipole.

$$G|_{dBi} = G|_{dBd} + 2.15$$

Be careful! Sometimes it is not clear if the antenna gain is given in dBi or dBd.

EIRP: Effective Isotropic Radiated Power

The effective isotropic radiated power normally termed as the effective radiated power (ERP) EIRP = Transmit power (fed to the antenna) + antenna gain

$$EIRP\mid_{dB} = P_{TX|dB} + G_{TX|dB}$$

Answers the questions:

How much transmit power would we need to feed an isotropic antenna to obtain the same maximum of radiated power? How "strong" is our radiation in the maximal direction of the antenna?

In the cases of limiting interference, ERP is used. So one can decrease power or use an antenna with less gain to limit ERP and in turn limit interference to other stations.

This is the more important one, since a limit on EIRP is a limit on the radiation in the maximal direction.

EIRP and the link budget



$$EIRP\mid_{dB} = P_{TX|dB} + G_{TX|dB}$$





Fading margin

Interference is subject to fading while noise is typically constant (averaged over a short time interval). To determine a fading margin, we statistially assume the desired signal is weaker than its median value 50% of the time and that the interfering signal is stronger that its median value 50% of the time. PL = the admissable path loss is ratio of the EIRP transmit power to the mean received power



Required C/N – another central concept



Example for link budget



Noise and interference limited links



What is the impact of distance between BSs?

CoChannel Interference will be discussed in Chapter 17 - Multiple Access



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