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# DISTRETE FOURIER TRANSFORM

## DFT PRESENTATION 1

### Using Harman Chapter 11

$$F_k = F\left(\frac{k}{NT_s}\right) = \sum_{n=0}^{N-1} f(nT_s)e^{-i2\pi nk/N} \quad (11.5)$$

**Definition of DFT and IDFT** Assume that a function  $f(t)$  is defined at a set of  $N$  points,  $f(nT_s)$  for  $n = 0, \dots, N - 1$  values, as shown in Figure 11.3. The DFT yields the frequency spectrum at  $N$  points by the formula

$$F_k = F\left(\frac{k}{NT_s}\right) = \sum_{n=0}^{N-1} f(nT_s) e^{-i2\pi nk/N} \quad (11.5)$$

for  $k = 0, \dots, N - 1$ . Thus,  $N$  sample points of the signal in time lead to  $N$  frequency components in the discrete spectrum spaced at intervals  $f_s = 1/(NT_s)$ . The Inverse DFT (IDFT) is defined as

$$f_n = f(nT_s) = \frac{1}{N} \sum_{k=0}^{N-1} F\left(\frac{k}{NT_s}\right) e^{i2\pi nk/N} \quad (11.6)$$

for  $n = 0, \dots, N - 1$ . The IDFT is used to re-create the signal from its spectrum.

# LECTURE OBJECTIVES

- Discrete Fourier Transform

$$X[k] = \sum_{n=0}^{N-1} x[n] e^{-j(2\pi/N)kn}$$

$$x[n] = \frac{1}{N} \sum_{k=0}^{N-1} X[k] e^{j(2\pi/N)kn}$$

- DFT from DTFT by frequency sampling
- DFT computation (FFT)
- DFT pairs and properties
  - Periodicity in DFT (time & frequency)

## DIFFERENCES TLH AND DSPF

$$F_k = F\left(\frac{k}{NT_s}\right) = \sum_{n=0}^{N-1} f(nT_s)e^{-i2\pi nk/N} \quad (11.5)$$

**T<sub>s</sub> is the time between samples      S = 1/T<sub>s</sub> samples/sec**

**Thus, F<sub>k</sub> values are frequencies and f values are given at a specific time nT<sub>s</sub>**

$$X[k] = \sum_{n=0}^{N-1} x[n]e^{-j(2\pi/N)kn}$$

**Here n and k are indices –**

**NO relation to physical time of frequency**

**GO OVER :**

**WEBSITE MATERIAL**

- HARMAN CHAPTER 11
- WEB VIDEOS FOR DSP

[DFT\\_FFT\\_TLH](#)

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