

# Ch. 1 Fundamental Concepts

Kamen and Heck

And

T.L. Harman

# Good Links

Good MATLAB Information and Help

<http://sceweb.sce.uhcl.edu/harman/>

MY WEB SITE

<http://www.mathworks.com/access/helpdesk/help/techdoc/matlab.shtml>

Kamen and Heck Website

<http://users.ece.gatech.edu/bonnie/book3/>

Fundamentals Signals Systems - Windows Internet Explorer

http://users.ece.gatech.edu/bonnie/book3/

Search the web (Babylon)

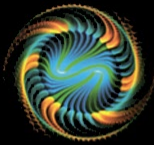
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McAfee

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Fundamentals Signals Systems



FUNDAMENTALS OF

SIGNALS AND SYSTEMS

USING THE WEB AND MATLAB®

THIRD EDITION

Home

Book Contents

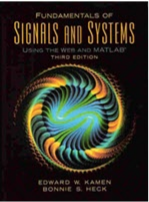
M-Files in Book

MATLAB™ Tutorial

On-Line Demos

Worked Problems

Instructor Notes



With the presentation at an introductory level, this book contains a comprehensive treatment of continuous-time and discrete-time signals and systems using demos on the Web, data downloaded from the Web, and illustrations of numerous MATLAB commands for solving a wide range of problems arising in engineering and in other fields such as financial data analysis. The third edition is a major revision of the previous edition in that the extent of the use of mathematics has been greatly reduced, practical applications involving downloaded data and other illustrations have been added, and the material has been reorganized in a significant way so that the flexibility in using the book in a one-quarter or one-semester course should be greatly enhanced.

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Desktop Libraries Links

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# 1.1 Continuous Time Signals

- $x(t)$  –a signal that is **real-valued** or scalar-valued function of the time variable  $t$ .
- When  $t$  takes on the values from the set of real numbers,  $t$  is said to be a continuous-time variable and the signal  $x(t)$  is said to be a **continuous-time signal** or an analog signal.

# Examples of Continuous Signals

- Figure 1.1 Speech Signal P2
  - Figure 1.2 Unit step and Unit ramp P2-3
  - Figure 1.3 Pulse Interpretation P3-4
  - Figure 1.4 Unit Impulse  $\delta(t)$
- 
- The step, ramp, pulse and unit impulse are the most important signals for testing a system.

- Example 1.1 Sum of Periodic Signals is periodic if “the two non-zero periods  $T_1=a$  and  $T_2=b$  are **commensurate**”

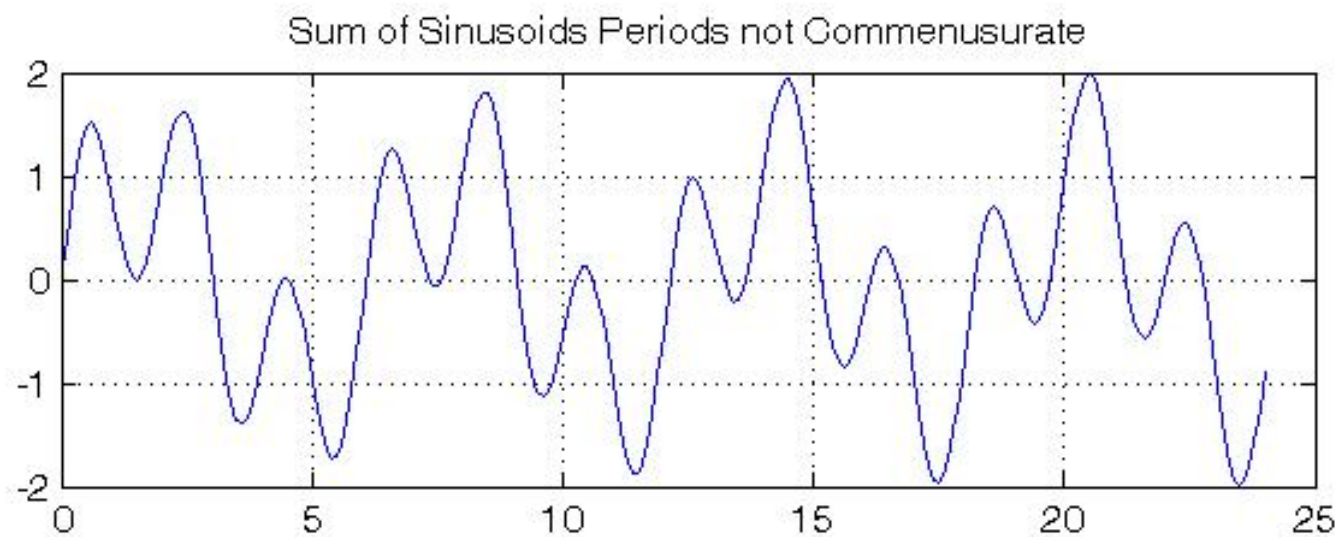
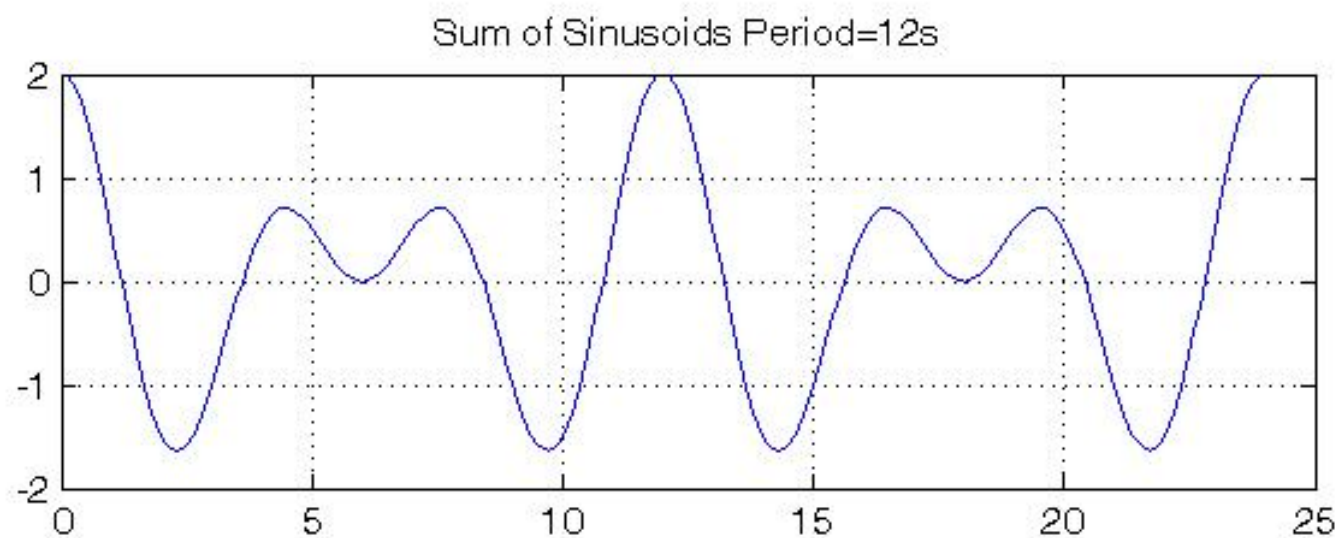
(if  $a/b$  is a rational number.)

- Figure 1.5 Periodic Signal P5
- $A \sin(\omega t + \varphi)$  is the most important signal
- $\omega = 2 \pi f \frac{\text{radians}}{\text{second}} \quad f = \frac{\text{cycles}}{\text{second}} \text{ (Hertz)}$
- The period  $T=1/f$  seconds or  $T= 2 \pi / \omega$  seconds

```

% K&H Chapter 1
% Periodic Ex 1.1
t=0:0.1:24;
y=cos(pi*t/2)+cos(pi*t/3);
% T1=4s, T2=6s; LCM=12; GCD(1/4,1/6)=1/12 Hz
%
figure(1)
subplot(2,1,1), plot(t,y)
grid
title('Sum of Sinusoids Period=12s')
y1=sin(t)+sin(pi*t);
subplot(2,1,2), plot(t,y1)
grid
title('Sum of Sinusoids Periods not Commensurate')

```





# More Continuous Time Signals

- Figure 1.6 Time-Shifted Signals P6
  - (A transmitted signal is time shifted at the receiver- and probably attenuated!)
- Figure 1.7 Triangular Pulse Function
- Figure 1.8 Rectangular Pulse Function P8
- Figure 1.9 Pulse train – approximate a computer clock signal
- These are all test signals for systems or approximations to useful signals!

## 1.1.6 Derivative of a Continuous-Time Signal

- A continuous time signal is said to be **differentiable** at a fixed point  $t_1$  if as  $h \rightarrow 0$  the limit from above is the same as the limit from below. P9-10
- $$\frac{dx}{dt} = \lim_{h \rightarrow 0} \frac{x(t+h) - x(t)}{h}$$
- Piecewise-continuous signals may have a derivative in the **generalized** sense.  $\delta(t)$

```
% PLOT K&H Figure 1.10 decaying sinusoid

%

t = 0:0.1:30;          % Plot from 0 to 30 seconds

x = exp(-0.1*t).*sin((2/3)*t);

%

figure(1)              % Figure number if multiple figures

plot(t,x)

axis([0 30 -1 1 ])     % Set appropriate axis limits

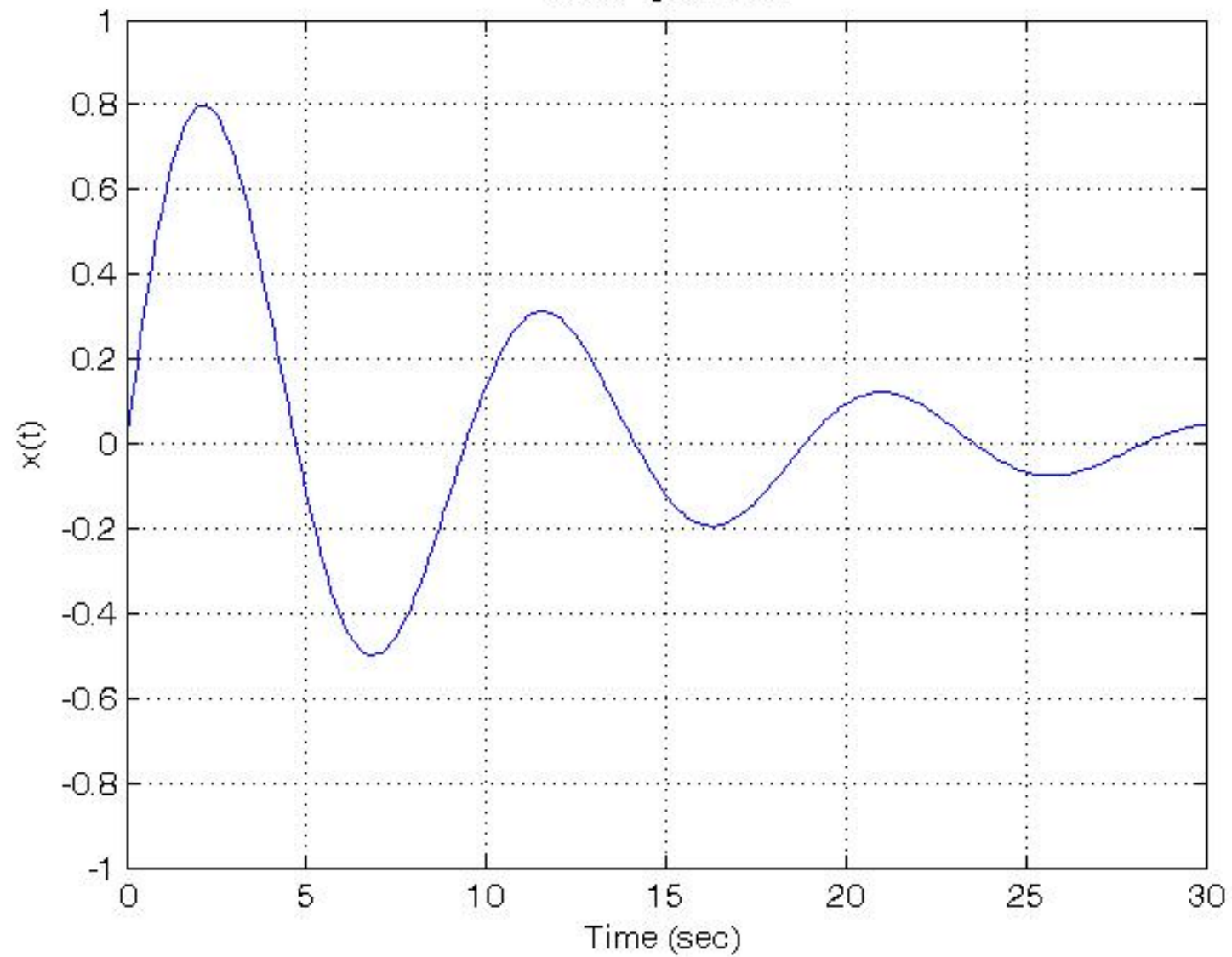
grid

title('K&H Figure 1.10')

xlabel('Time (sec)')

ylabel('x(t)')
```

K&H Figure 1.10



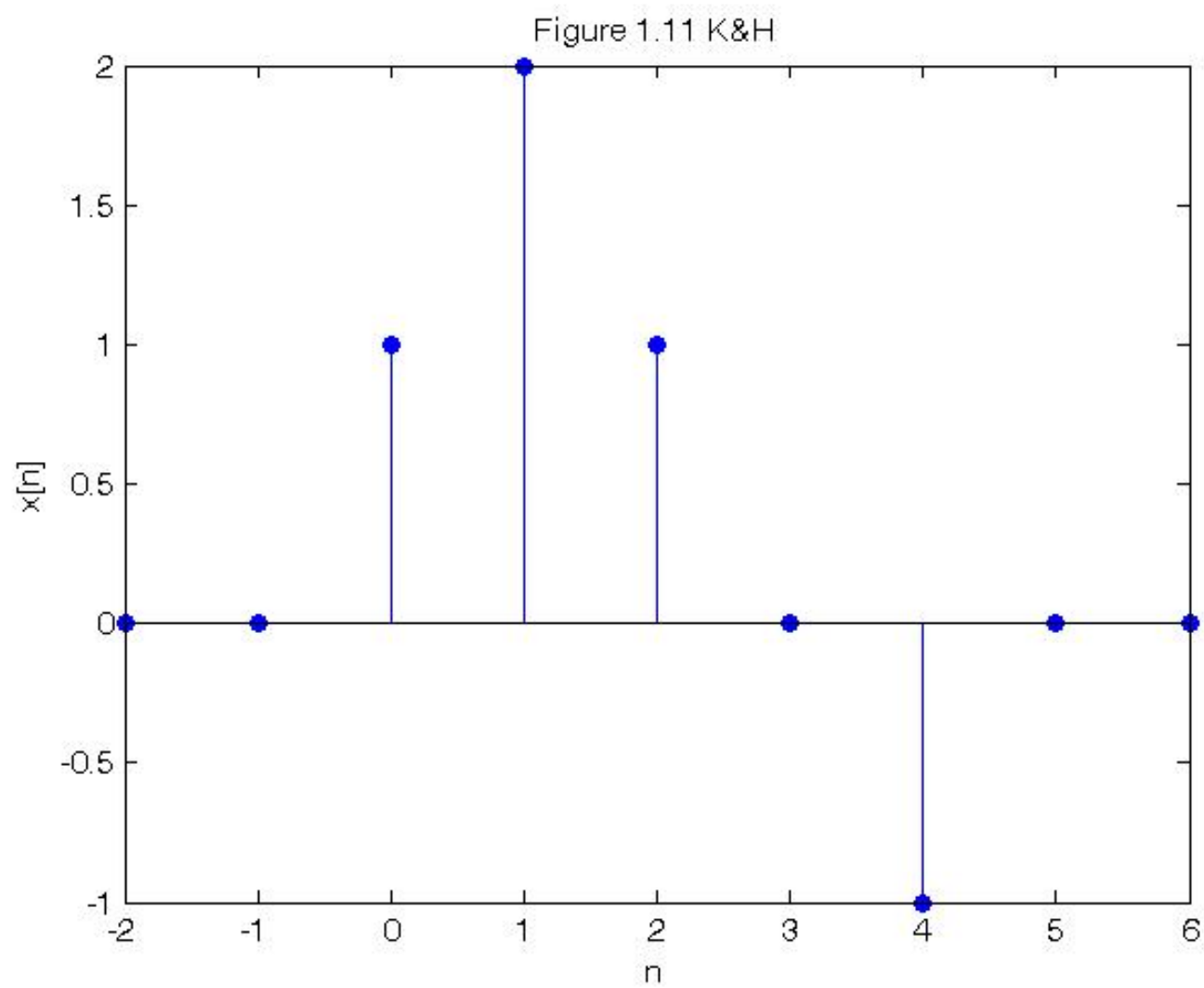
```

% Use MATLAB to plot using STEM Figure 1.11 K&H
n = -2:6;           %Index -2, -1, 0, ... 6 (9 values)
% x[0] =1, x[1]=2,x[2]=1, x[3]=0, x[4]= -1; others are zero
%
x= [0 0 1 2 1 0 -1 0 0] ;
figure(1)
stem (n,x,'filled'); % Plot Discrete with filled circles
title('Figure 1.11 K&H')
xlabel ('n')
ylabel ('x[n]')

```

The result using STEM is Figure 1.12 Page 13.

This could represent a digital signal since the amplitude and index values are quantized.



>>help stem    % Use the help often!

**stem**    Discrete sequence or "stem" plot.

stem(Y) plots the data sequence Y as stems from the x axis terminated with circles for the data value. If Y is a matrix then each column is plotted as a separate series.

stem(X,Y) plots the data sequence Y at the values specified in X.

stem(...,'filled') produces a stem plot with filled markers.

stem(...,'LINESPEC') uses the linestyle specified for the stems and markers. See PLOT for possibilities.

See also plot, bar, stairs.

Reference page in Help browser    **Use this for more information!**  
**doc stem    (Active Link from help stem screen)**

# More Discrete Time Signals

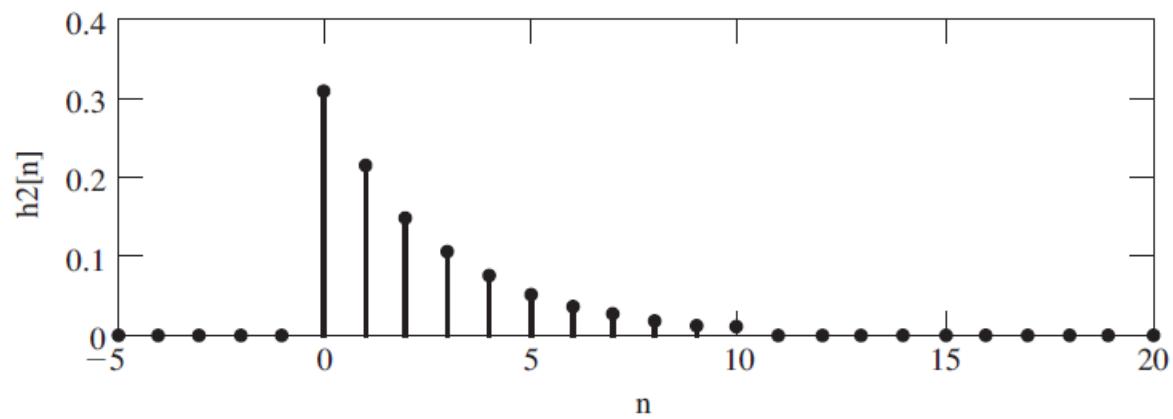
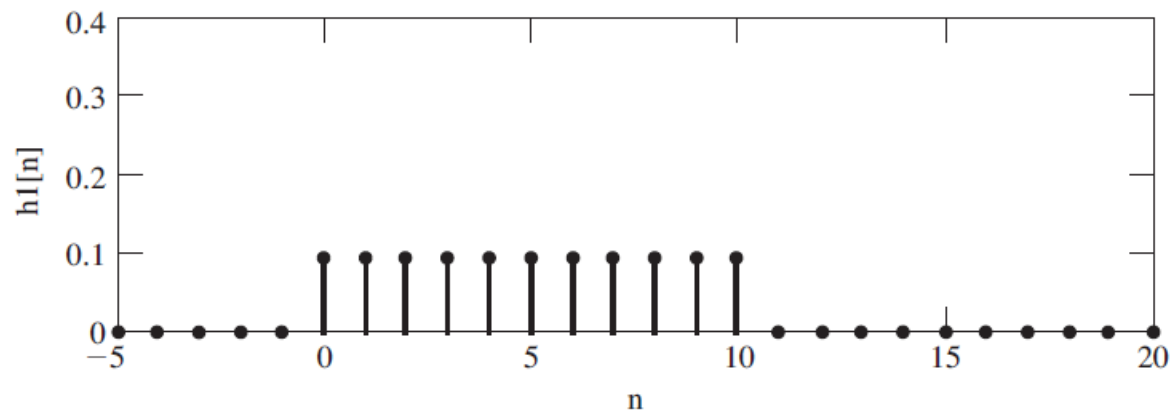
- Sampling
  - $x[n] = x(t) |_{t=nT} = x(nT)$
  - Example—a switch is closed every  $T$  seconds
  - Using “ $T$  seconds” brings in the “real world”.
- Unit pulse—  $\delta(0)$ —Figure 1.17
- Periodic Discrete Time Signals—Figure 1.18a,b
- F1.18a repeats every 6 cycles
- Discrete Time Rectangular Pulse Figure 1.19



# More Discrete Time Signals (2)

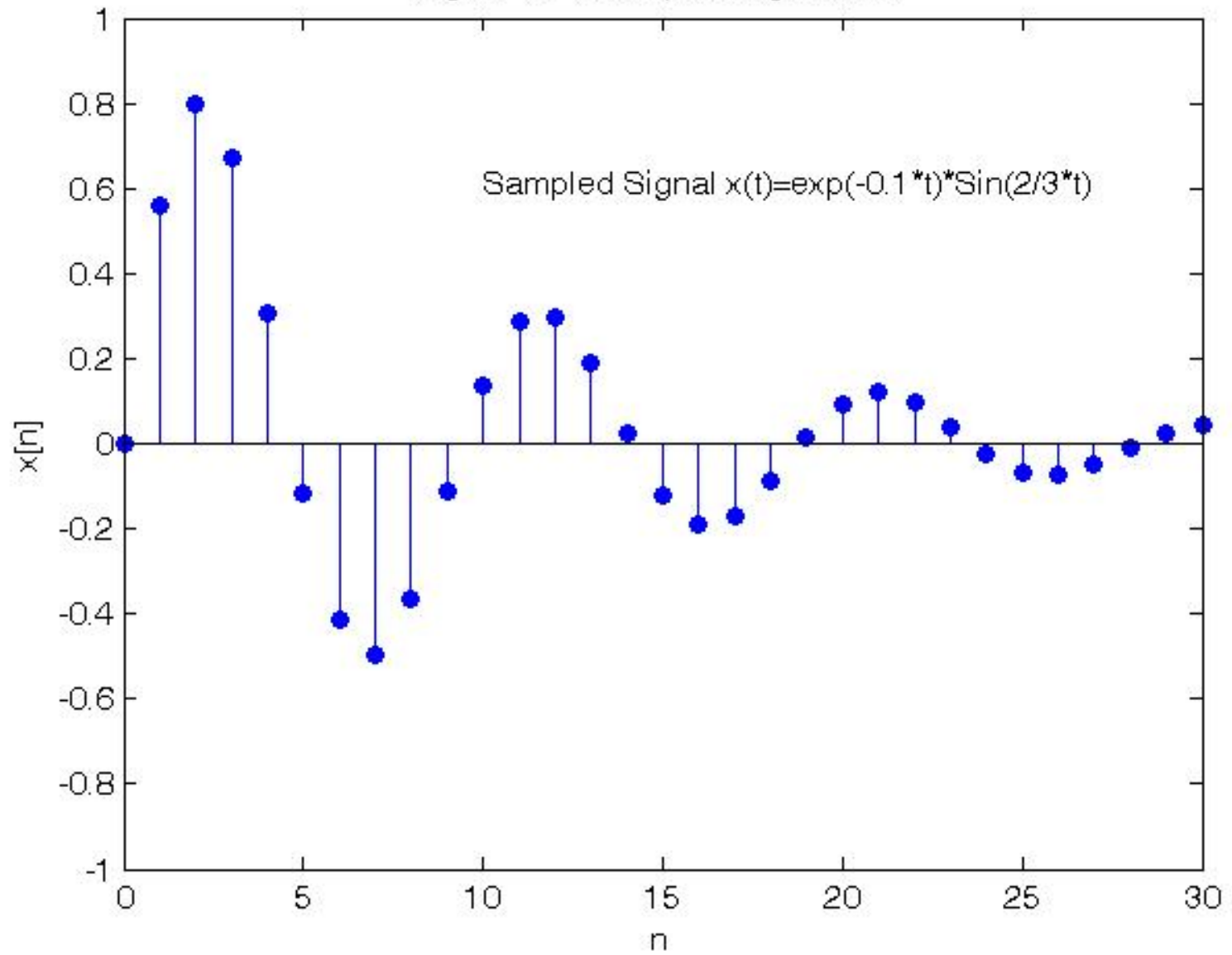
- **Digital Signals**

- Let  $\{a_1, a_2, \dots, a_N\}$  be a set of  $N$  real numbers.
- A **digital signal**  $x[n]$  is a discrete-time signal whose values belong to the finite set above.
- A **sampled continuous time signal** (ideal case) is not necessarily a “digital signal”. Digital is quantized in time AND amplitude – i.e a computer value.
- A **binary signal** is restricted to values of 0 and 1.



```
% K&H Figure 1.14    Compare this to Figure 1.10
%
n=0:30;
x = exp(-.1*n).*sin(2/3*n);
stem(n,x,'filled')
axis([0 30 -1 1]);
ylabel('x[n]')
xlabel('n')
title('Figure 1.14-Compare Figure 1.10')
gtext('Sampled Signal  $x(t)=\exp(-0.1*t)*\sin(2/3*t)$ ')
```

Figure 1.14-Compare Figure 1.10



# Downloading Discrete-Time Data from the Web P18

- Discrete-time data = a **time series**
- Time series data on websites can often be loaded into spreadsheets.
- If the spreadsheet data can be saved in csv (comma-separated value) formatted files, MATLAB will be able to read the file.
- OPTIONAL FOR US

# Price Data for QQQ

- QQQ data is the historical data for an index fund, whose value tracks the stock price of 100 companies.
- Go to <http://finance.yahoo.com>
- Near the top of the page enter QQQQ and click “GO”.
- In the left hand column click on “historical prices”.
- Click on “Download to Spreadsheet”.
- Example 1.2.
- (NOTE: Some things have changed a little since the book was printed but this still works.)

# 1.3 Systems

- A system is a collection of one or more devices, processes, or computer-implemented algorithms that operates on an input signal  $x$  to produce an output signal  $y$ .
- When the inputs and outputs are continuous-time signals, the system is said to be a continuous-time system or an analog system.
- When inputs are discrete-time signals, the system is said to be a discrete-time system.

**READ PAGES 21 -24 CAREFULLY!**

SYSTEM EXAMPLES-MECHANICAL, ELECTRICAL,  
BIOLOGICAL

SIGNAL ANALYSIS—In the time domain or frequency domain  
rise time, amplitude, power, etc. in Time.  
Frequency spectrum in frequency. (Fourier)

MATHEMATICAL MODELS of SYSTEMS – IDEAL  
differential equations or difference equations (Time)  
Transfer function representations (Fourier, Laplace,  $z$ )

INPUT/OUTPUT - Time or Frequency  
STATE-SPACE - Input, state, and output



# 1.4 Examples of Systems

- RC Circuit P24

This is a model for input stages of many analog electronic systems.

The RC acts as a low-pass filter and attenuates high frequencies in the input signal.

- Mass-Spring-Damper System P26

Why is the world a 2<sup>nd</sup> Order system (almost)?

- Moving Average Filter (Discrete) P 27

- This is also a low-pass filter that acts to “smooth” the data.
- See Example 1.4

# 1.5 Basic System Properties

- Systems are classified as follows
  - Analog or Discrete (Digital)
  - Linear or Nonlinear
  - Time Invariant (shift invariant) or not
  - All analog physical systems are causal (as far as we know!)
- Signals can be Analog or discrete (digital) and
  - continuous or discontinuous
  - Periodic or not
  - Even or Odd

# Linearity

- A system is **additive** if for  $x_1(t)$  and  $x_2(t)$  (inputs), the response to the **sum** of the inputs is the **sum** of the individual outputs.
- A system is **homogeneous** if the output for input  $ax(t)$ , where  $a$  is a scalar, is  $ay(t)$ .
- A system is **linear** if it is **additive and homogenous**.
- That is, if  $x_1(t) \rightarrow y_1(t)$ , and  $x_2(t) \rightarrow y_2(t)$ , and  $a_1$  and  $a_2$  are scalars, then a system is linear if the input

$$x(t) = a_1x_1(t) + a_2x_2(t)$$

produces the output

$$y(t) = a_1y_1(t) + a_2y_2(t).$$

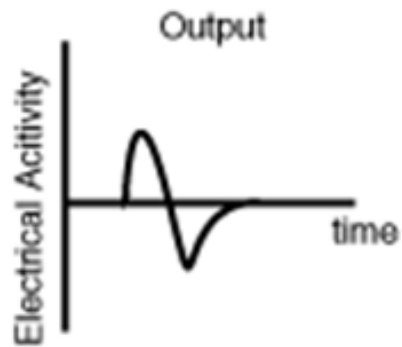
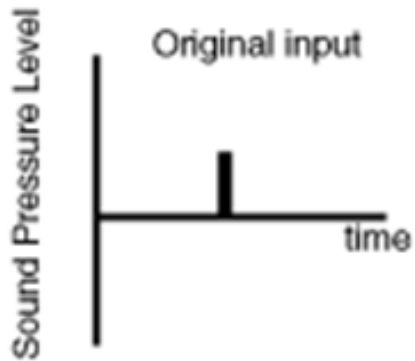
## Linear Systems Theory

### Professor David Heeger

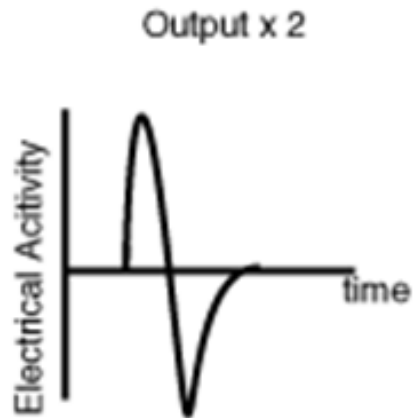
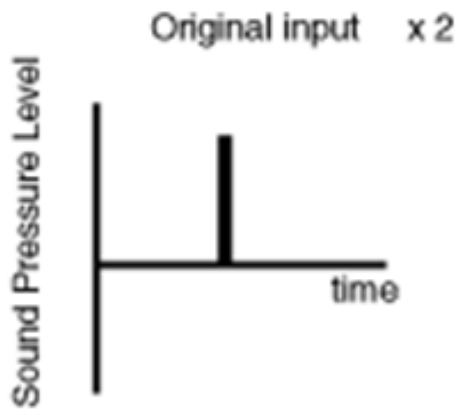
Characterizing the complete input-output properties of a system by exhaustive measurement is usually impossible. When a system qualifies as a *linear system*, it is possible to use the responses to a small set of inputs to predict the response to any possible input. This can save the scientist enormous amounts of work, and makes it possible to characterize the system completely.

- The challenge of characterizing a complex systems
- Simple linear systems
  - Homogeneity - Double Input- Double Output
  - Additivity - Sum of Outputs for Sum of Inputs
  - Superposition - THE BIG ONE
  - homogeneity and additivity = LINEAR

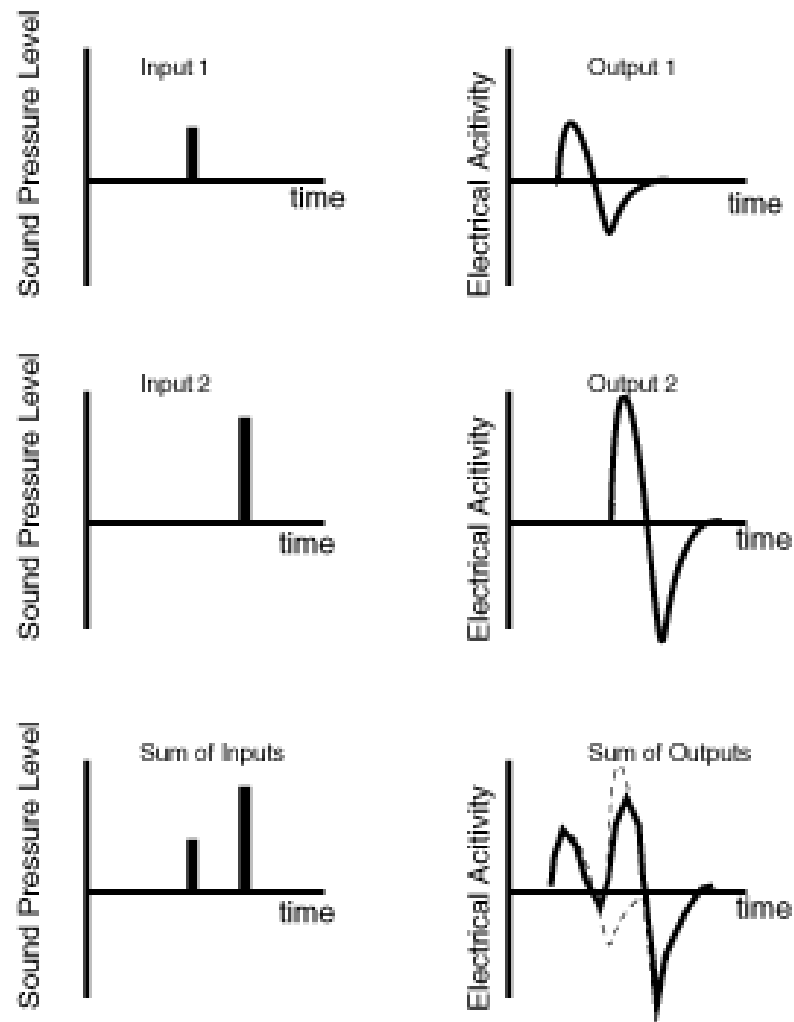
## Scalar Rule



Think of  
 $F = -kx$   
Spring



## Additivity

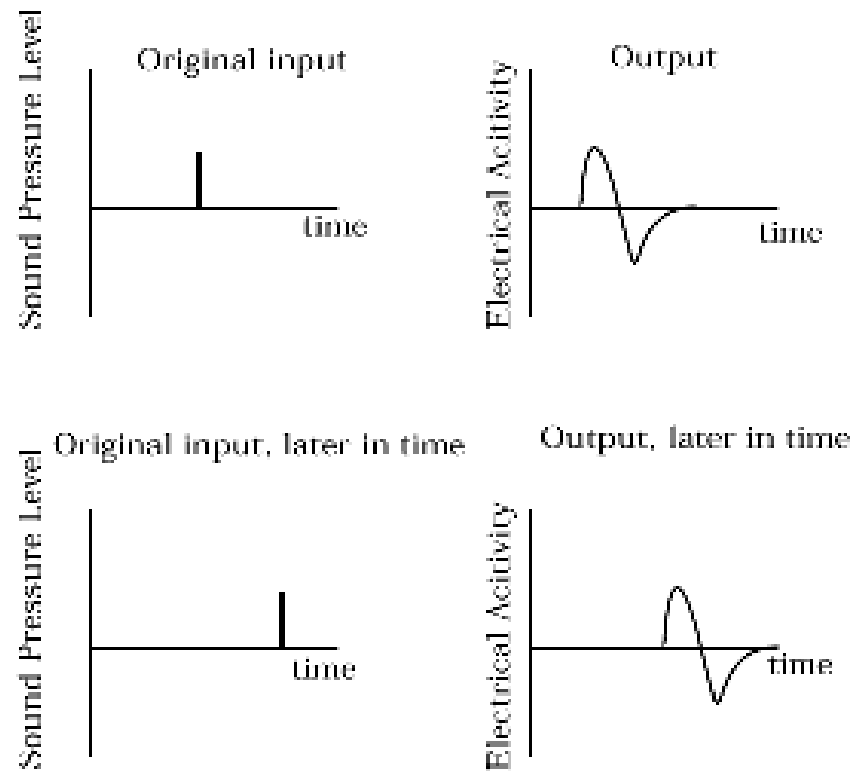


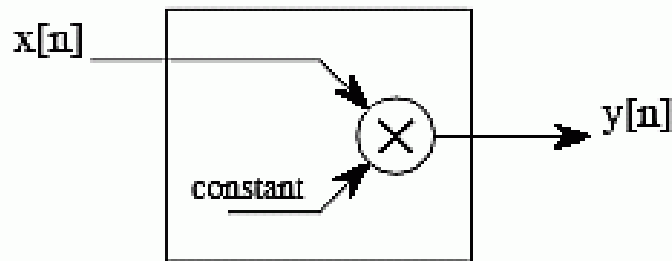
- Shift-invariance

- Decomposing a signal into a set of shifted and scaled impulses
- The impulse response function
- Use of sinusoids in analyzing shift-invariant linear systems
- Decomposing stimuli into sinusoids via Fourier Series
- Characterizing a shift-invariant system using sinusoids



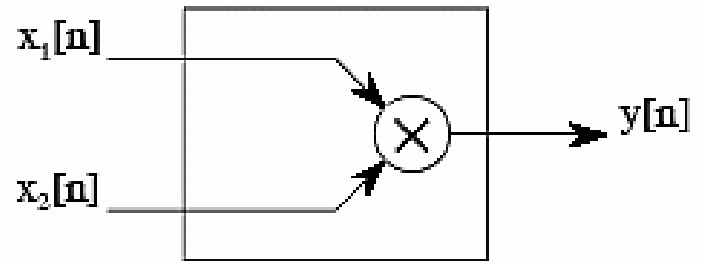
## Shift-Invariance Rule





Linear

a. Multiplication by a constant



Nonlinear

b. Multiplication of two signals

FIGURE 5-9

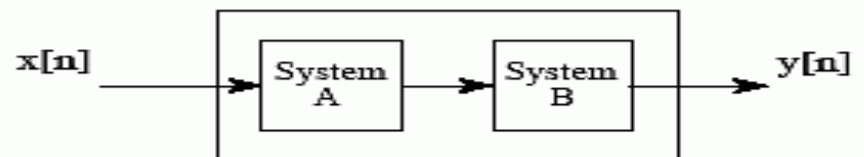
Linearity of multiplication. Multiplying a signal by a constant is a linear operation. In contrast, the multiplication of two signals is nonlinear.

Smith

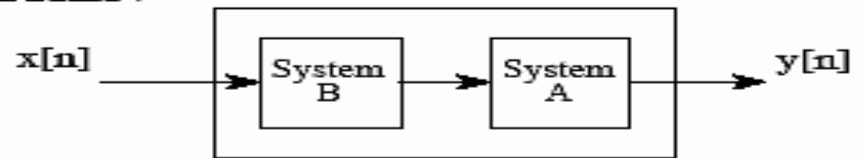
FIGURE 5-7

The commutative property for linear systems. When two or more linear systems are arranged in a cascade, the order of the systems does not affect the characteristics of the overall combination.

IF

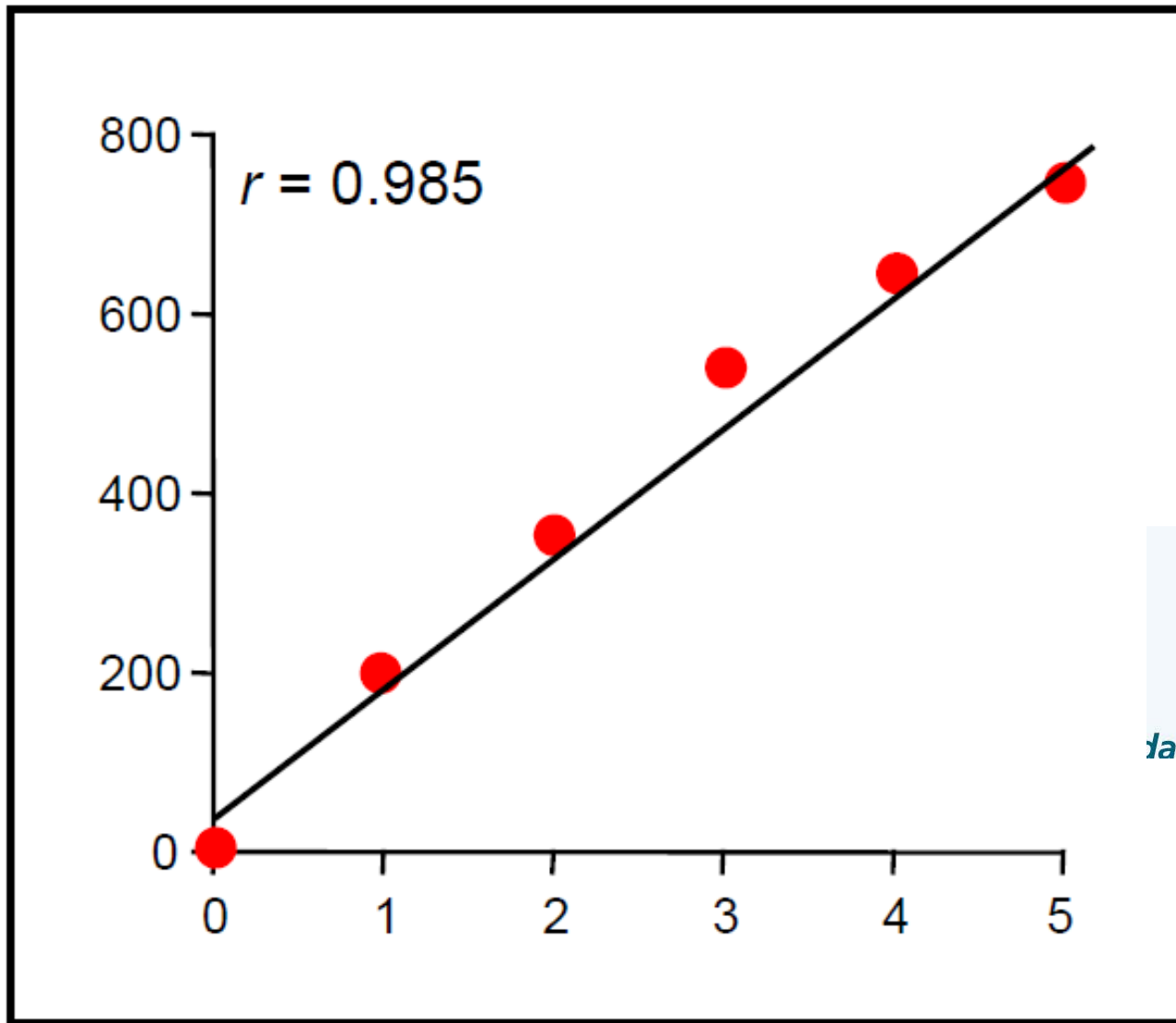


THEN



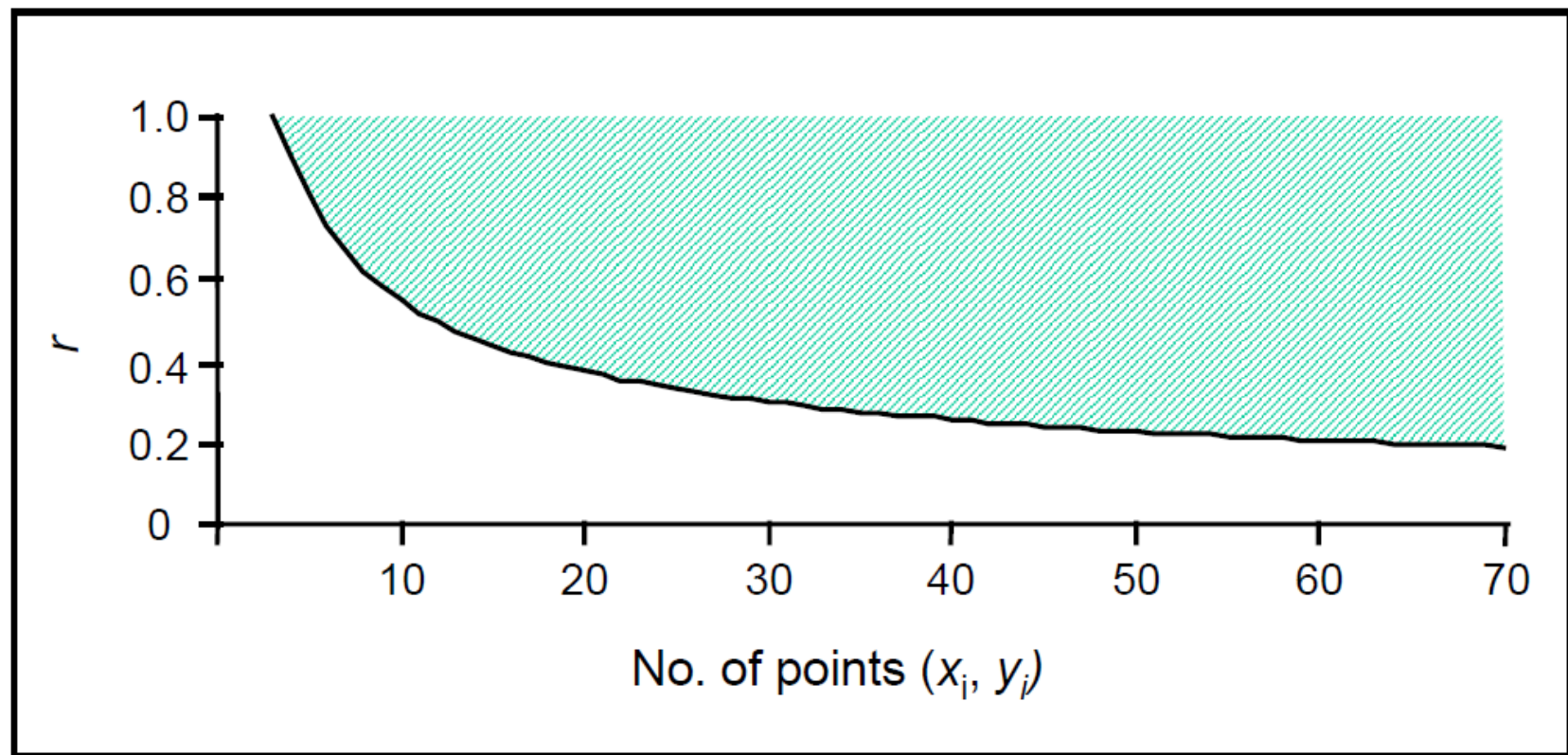
## ☐ LINEAR

- ☐ Systems described by Linear differential or difference equations
- ☐ Passive Circuits  $R$ ,  $L$ ,  $C$  and linear amplifiers and filters
- ☐ Differentiation and integration or difference or running sum
- ☐ Small perturbations in an otherwise nonlinear system



*yards*

**a) Non-linearity**



- NON LINEAR

- ❑ NO STATIC LINEARITY I.E, NOT  $Y=M X$  such as  $P=v^2 R$
- ❑ NO SINUSOIDAL FIDELITY – PEAK DETECTION, SQUARING, CLIPPING, FREQUENCY DOUBLING
- ❑ Systems with hysteresis, saturation, or a threshold
- ❑ DIODES FOR EXAMPLE

## Shockley diode equation

$$I = I_S \left( e^{V_D / (n V_T)} - 1 \right) ,$$

$I$  is the diode current,

$I_S$  is the reverse bias [saturation current](#),

$V_D$  is the voltage across the diode,

$V_T$  is the [thermal voltage](#) , and

$n$  is the *ideality factor*.

$I_S$  and  $nV_T$  are constants.

Let's Linearize the Diode equation using Taylor's series near  $V_D=0$



MacLaurin series:

$$\begin{aligned} e^x &= f(0) \frac{x^0}{0!} + f'(0) \frac{x^1}{1!} + f''(0) \frac{x^2}{2!} + f'''(0) \frac{x^3}{3!} + f^{(4)}(0) \frac{x^4}{4!} + \dots \\ &= \frac{x^0}{0!} + \frac{x^1}{1!} + \frac{x^2}{2!} + \frac{x^3}{3!} + \frac{x^4}{4!} + \frac{x^5}{5!} + \dots \\ &= \sum_{n=0}^{\infty} \frac{x^n}{n!} \end{aligned}$$

For small  $x$  - close to the origin assume  $x^2 \ll x$  so

$$e^x \sim 1 + x \quad \text{where } x \text{ here is } \frac{V_D}{nV_T}$$

The result is

$$I \sim I_s \frac{V_D}{nV_T} \quad \text{Linear in } V_D$$

# Other System Properties

- Time Invariance
  - A system is time invariant or constant if the response for the input  $x(t-t_1)$  is  $y(t-t_1)$ .
- Causality
  - A system is said to be causal or nonanticipatory if the output response to input  $x(t)$  for  $t=t_1$  does not depend on values of  $x(t)$  for  $t>t_1$  (ie, future inputs).

Important problems – whether I assign them or not !

1.2 Spacing when plotting or sampling

1.18 Linearity – Integral, derivative

1.21 Dead zone – Nonlinear

1.23 Save some work – Impulse response is the derivative  
of the step response